

$$f(x) = -(x^2 - 16)^2 (3x - 7)^5$$

Degree:

Real roots:

Imaginary roots:

$$f(x) = -(x^2 - 16)^2 (3x - 7)^5$$

Degree: $4 + 5 = \boxed{9}$

Real roots:

$$x^2 - 16 = 0$$

$+16 \quad +16$

$$\sqrt{x^2} = \sqrt{16}$$

$$\boxed{x = \pm 4} \text{ multiplicity of 2}$$

$$3x - 7 = 0$$

$+7 \quad +7$

$$\frac{3x}{3} = \frac{7}{3}$$

$$\boxed{x = \frac{7}{3}}$$

multiplicity of 5

Imaginary roots:

No imaginary roots

9th degree has 9 real roots

$$f(x) = x^4 (x^2 + 36)^2 (2x + 6)^3$$

Degree:

Real roots:

Imaginary roots:

$$f(x) = x^4 (x^2 + 36)^2 (2x + 6)^3$$

Degree: $4 + 4 + 3 = \boxed{11^{\text{th}}}$

Real roots:

$$2x + \cancel{6} = 0$$

$\quad -6 \quad -6$

$$\frac{\cancel{2}x}{2} = \frac{-6}{2}$$

$$\boxed{x = -3}$$

Multiplicity
of 3

$$\boxed{x = 0}$$

Multiplicity of 4

Imaginary roots:

$$x^2 + \cancel{36} = 0$$

$\quad -36 \quad -36$

$$\sqrt{x^2} = \sqrt{-36}$$

$$\boxed{x = \pm 6i}$$

Multiplicity
of 2

11^{th} degree has
11 complex roots

Create polynomial equations for each degree and set of complex roots

- 1) 2nd degree & 2 imaginary roots
- 2) 3rd degree, 1 real root & 2 imaginary roots
- 3) 4th degree & 3 real roots
- 4) 5th degree & 1 real root

Create polynomial equations for each degree and set of complex roots

1) 2nd degree & 2 imaginary roots

$$f(x) = x^2 + 4 \quad \text{or} \quad g(x) = x^2 + 10$$

2) 3rd degree, 1 real root & 2 imaginary roots

$$f(x) = x(x^2 + 9) \quad \text{or} \quad g(x) = (x - 8)(x^2 + 20)$$

3) 4th degree & 3 real roots

$$f(x) = x^2(x + 2)(x - 9) \quad \text{or} \quad g(x) = (x + 7)^2(x^2 - 25)$$

4) 5th degree & 1 real root

$$f(x) = (x - 3)^5 \quad \text{or} \quad g(x) = 8x^5$$